

# Optimized Rendezvous of a Quadrotor

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# Motivation



Source : Skycatch Inc.



Source : GRASP lab



Source : ETH Zurich



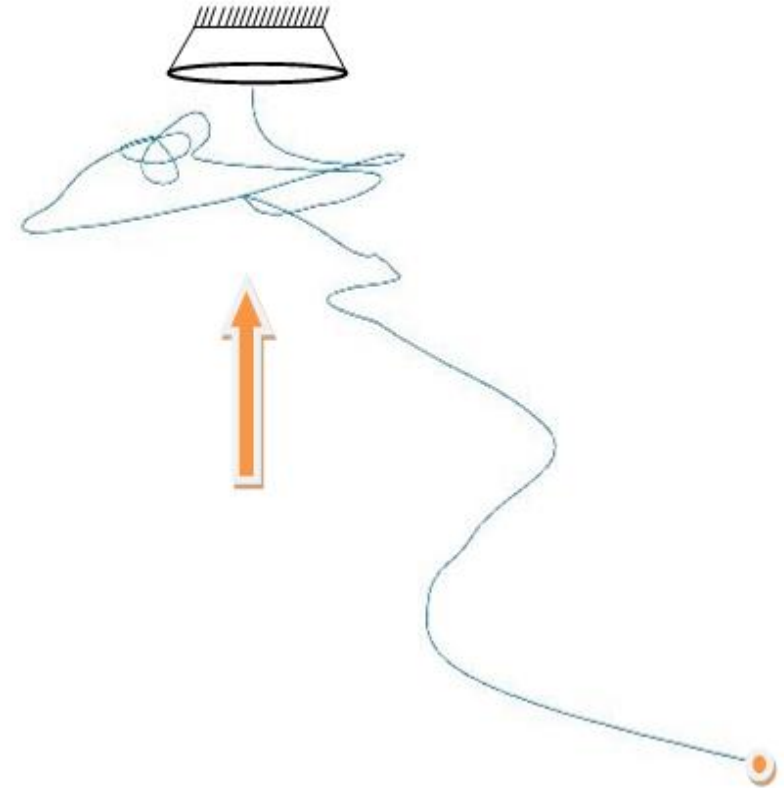
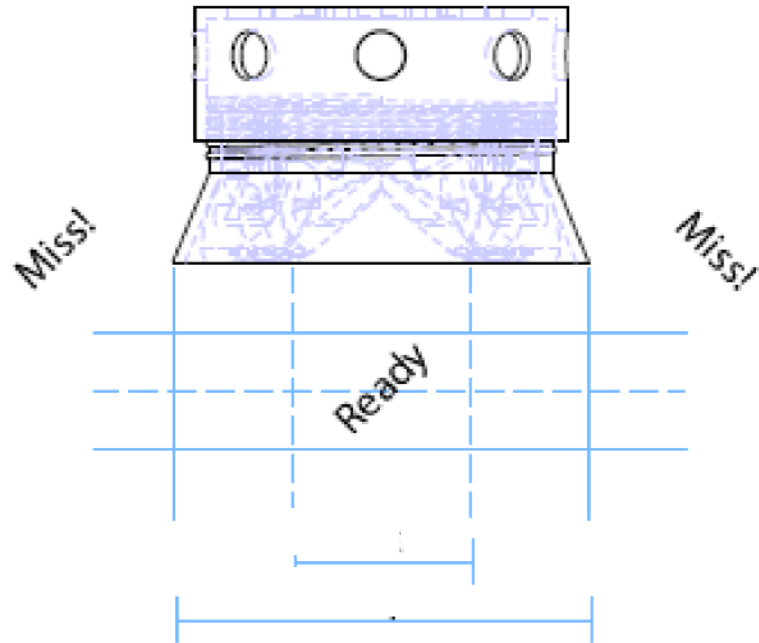
Source : A passive gripper mechanism .. [DeGol et. al]

- Assume perfect position sensing
- Disturbances present due to wind
- Uncertainty in attaining the desired velocity vector
- Path planner is needed to find desired position



# Related Work and New Approach

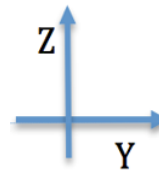
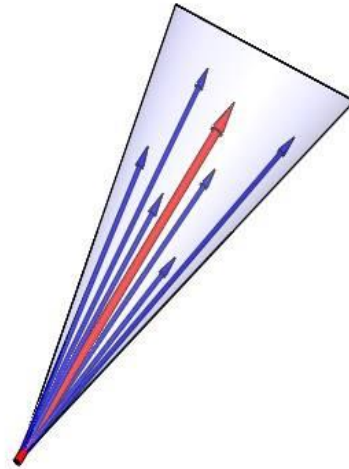
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# Method Intuition:

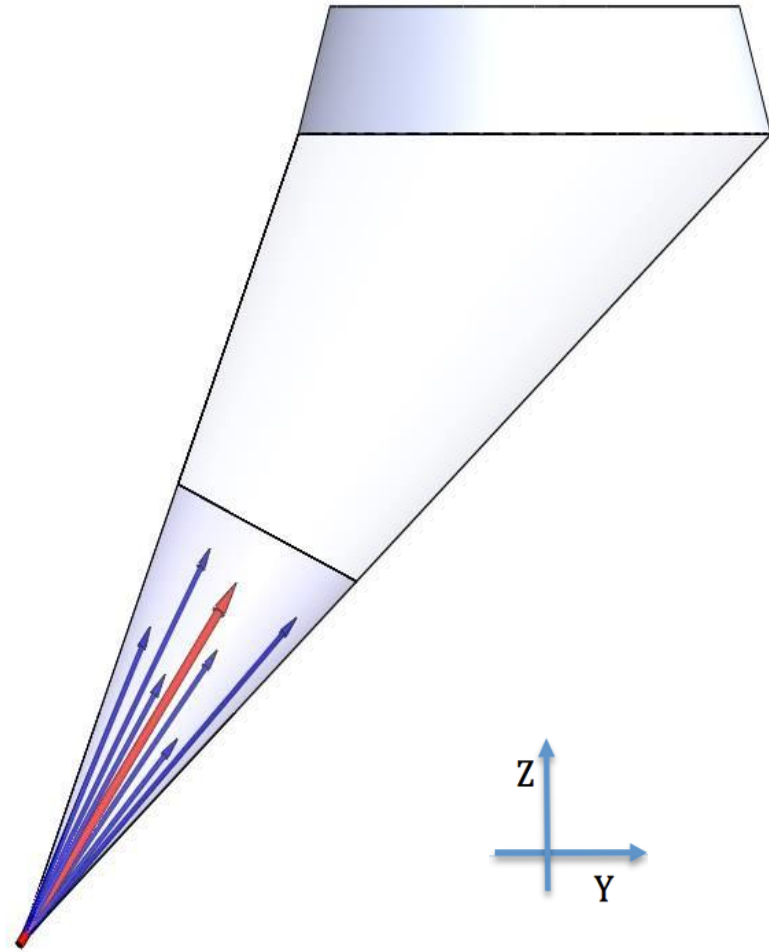
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- **Desired** velocity vector
- Other **possible velocity** vectors



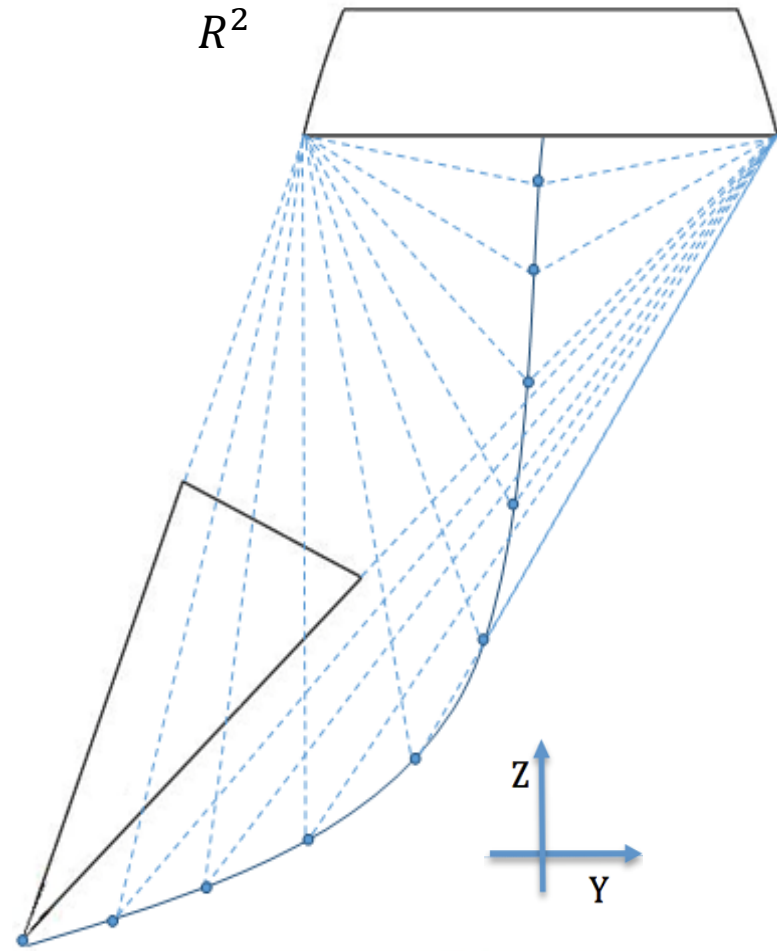
# Method Intuition:

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# Method Intuition:

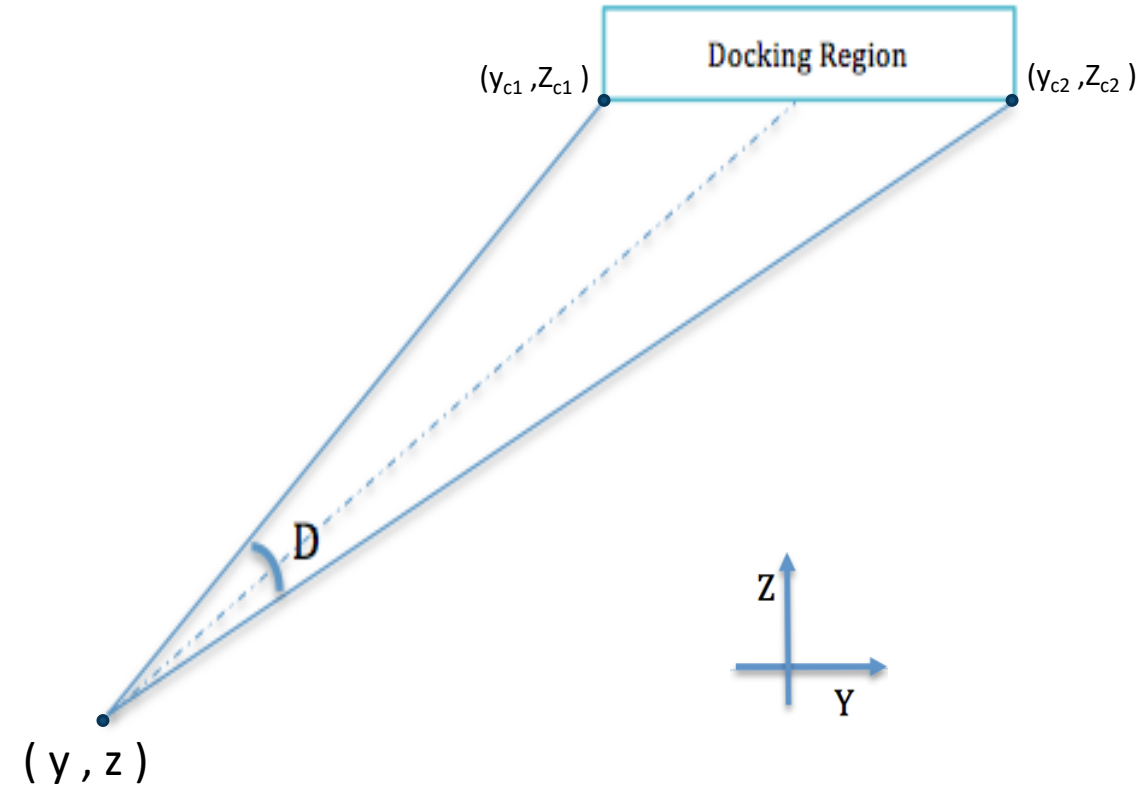
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# Method Intuition: The Difference function

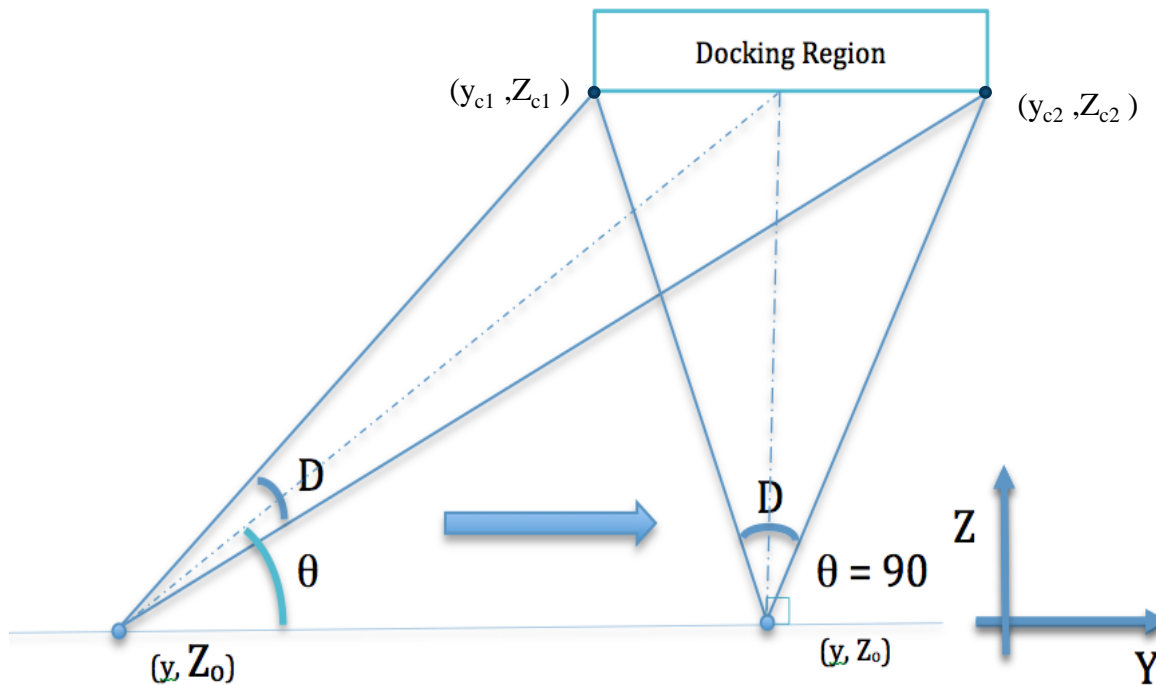
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- We define a “**D**ifference Angle”,  
 $D : \mathbb{R}^2 \rightarrow [0, \pi]$

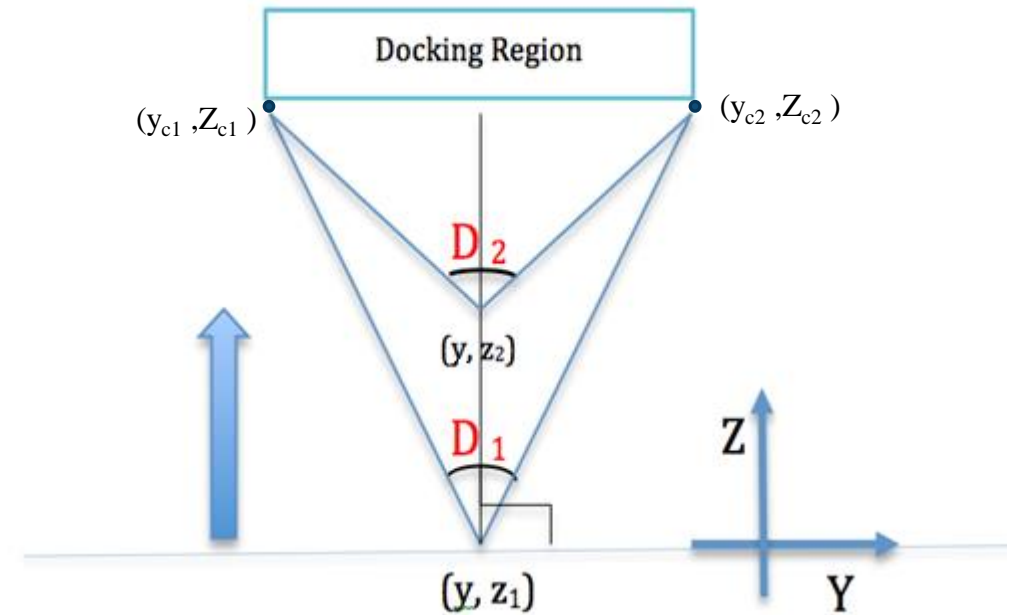


# Method Intuition: Difference Space Properties

- Claim 1:  $\forall Z_o, \theta \rightarrow 90^\circ, D_\theta = \max \{D(Z_o, \theta)\}$ . [ Figure 1 ]
- Claim 2: If pairs  $(Z_1, \theta_1)$  and  $(Z_2, \theta_2)$  are such that  $\theta_1 = \theta_2 = 90^\circ$  and  $Z_c > Z_2 > Z_1$ , then,  $D_2 > D_1$  where  $D_1 = D(Z_1, \theta_1)$  and  $D_2 = D(Z_2, \theta_2)$ . [ Figure 2 ]



**Figure 1.** Comparison of  $D(y, Z_o, \theta)$  as  $\theta \rightarrow 90^\circ$



**Figure 2.** Comparison of  $D(y, z)$  as  $z$  increases when  $\theta = 90^\circ$





# Objective Function

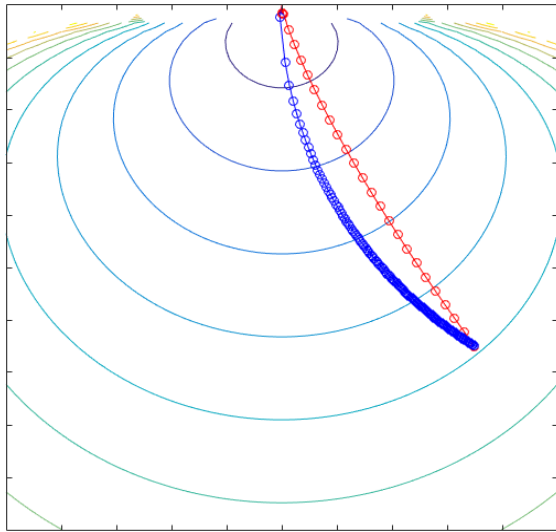
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Difference angle increases the robustness, but in order to decrease the time to dock, we employ a new cost function assuming a constant velocity:

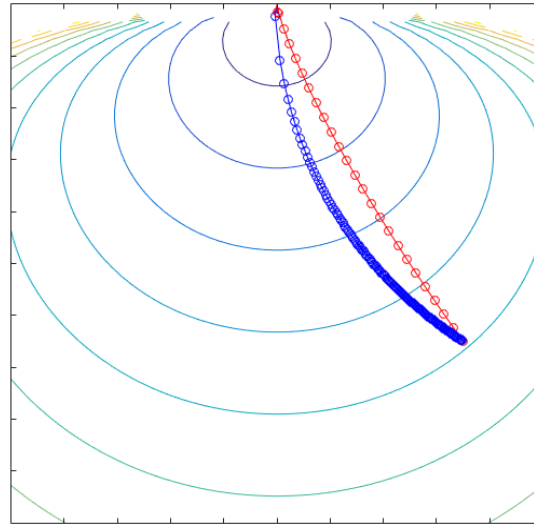
$$J = A \left( \frac{1}{D} \right) + B \|x_m - x_q\|$$



# Method Intuition

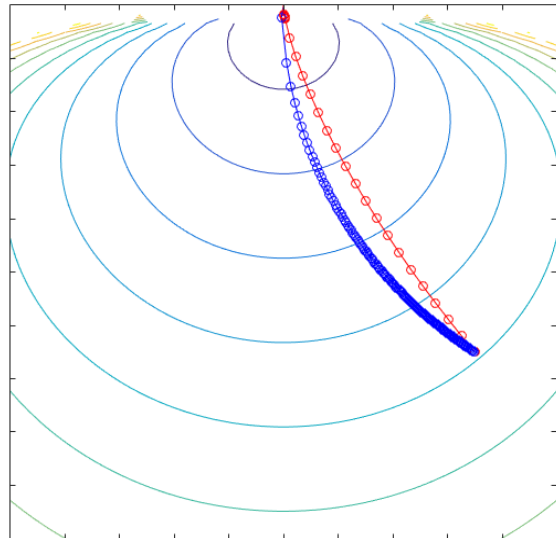


$A = 0$   
 $B = 50$

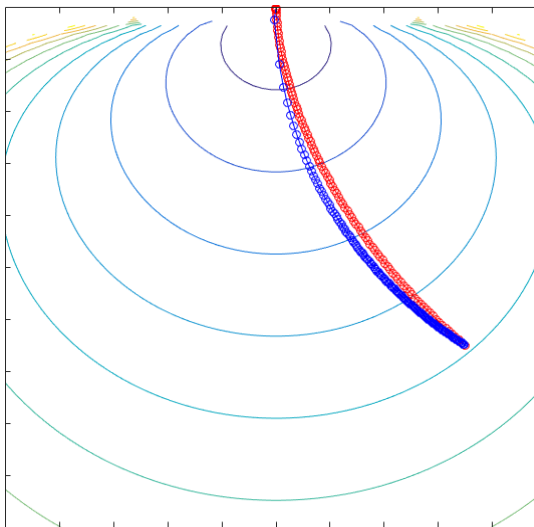


$A = 1$   
 $B = 50$

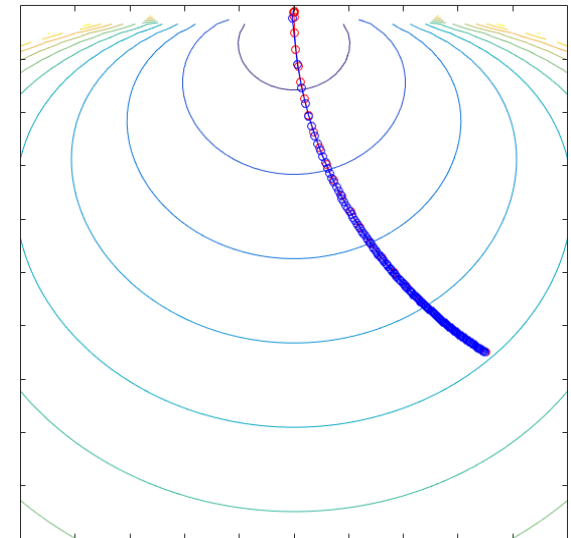
 Proposed method  
 Diff. Angle method



$A = 2$   
 $B = 50$



$A = 8$   
 $B = 50$



$A = 50$   
 $B = 0$

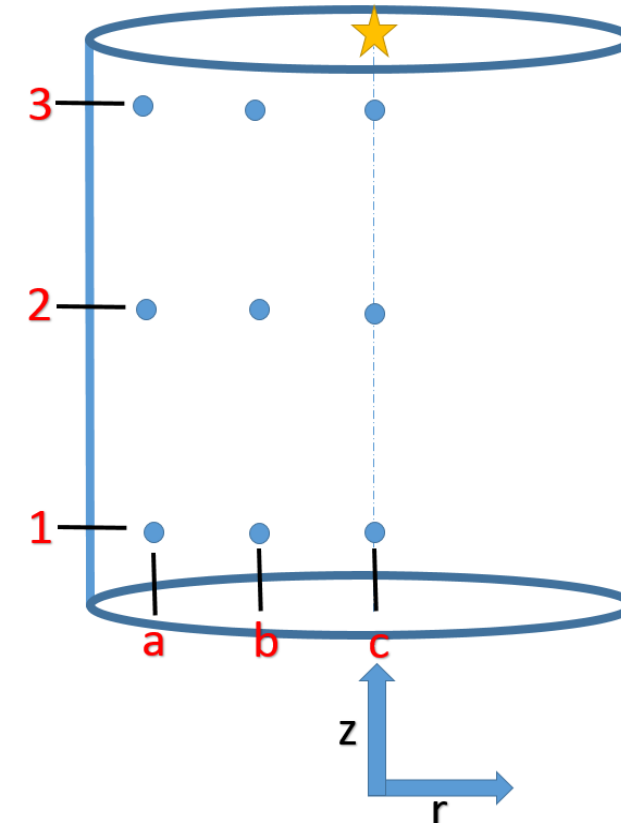


# Monte Carlo Experiments

Experiment I Setup:

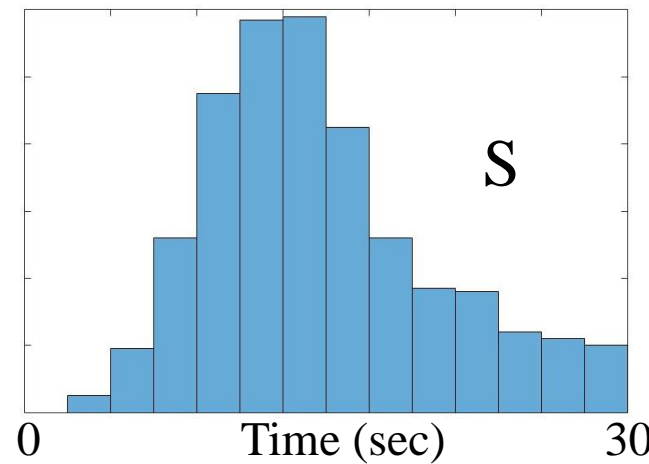
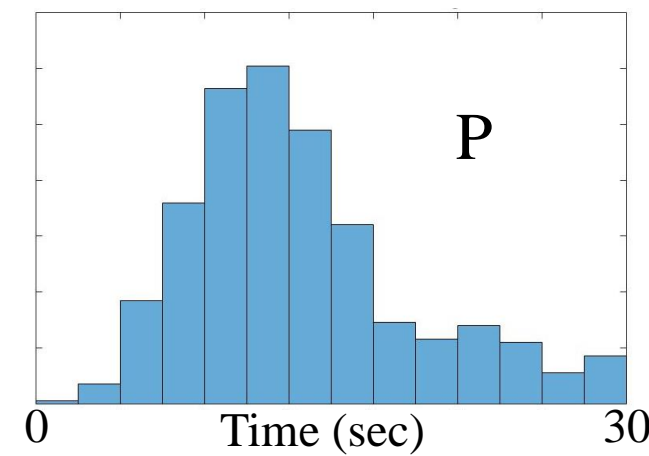
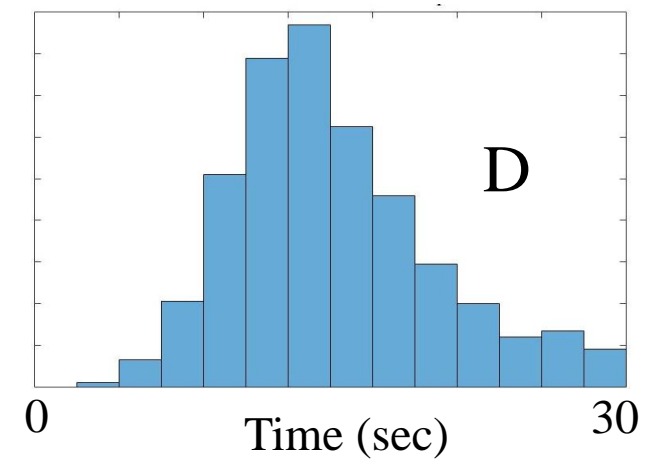
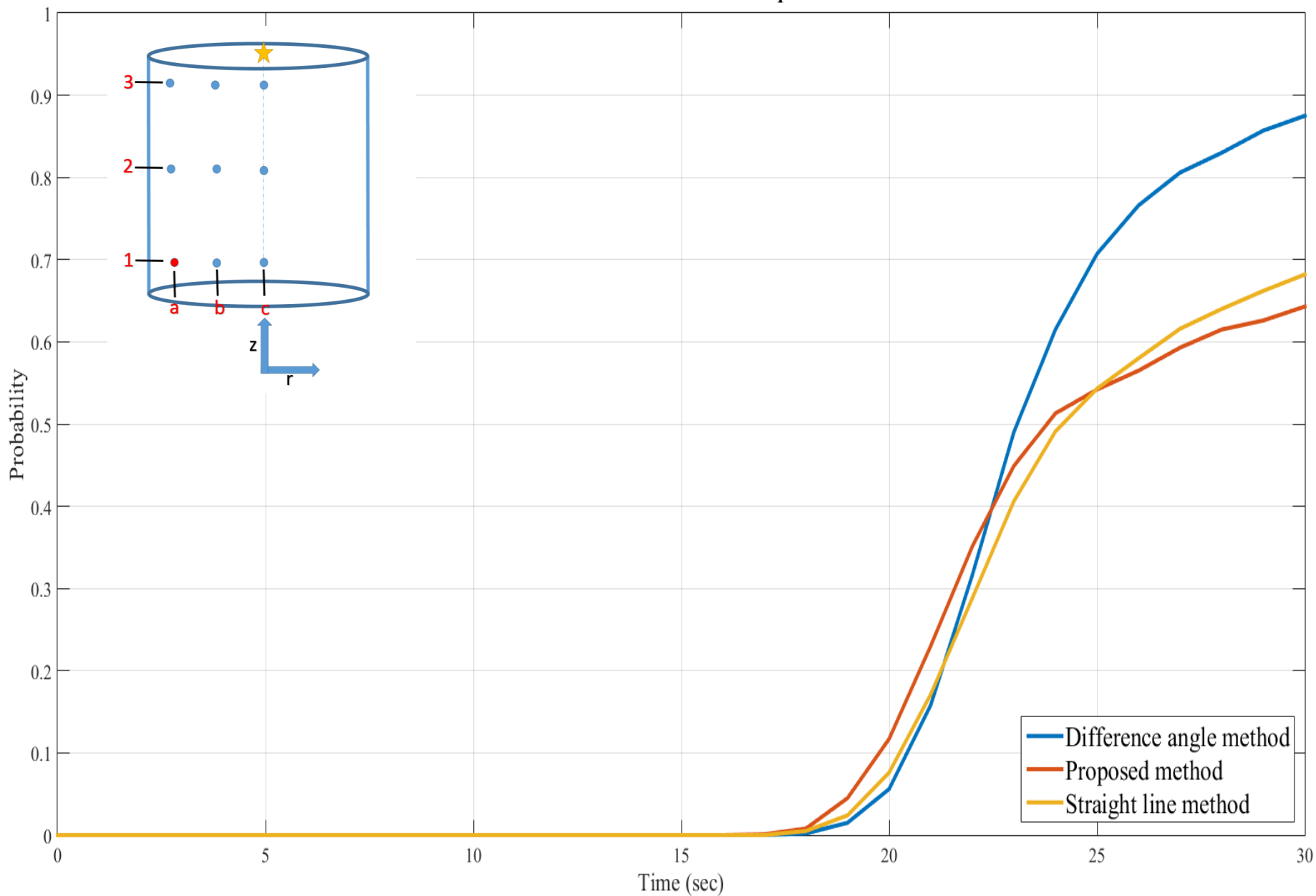
Experiment I
PD Controller (Constant Gains)
Disturbance: Mean=0, Variance=0.001
Constant Planner Gain
Docking region limit 0.01
Proposed method weights (A = 1, B =50)
Straight line method weights (A = 0, B =1)
Number of Monte Carlos runs : 1000

$a_1(0.95, 0.15)$	$a_2(0.95, 1)$	$a_3(0.95, 1.85)$
$b_1(0.5, 0.15)$	$b_2(0.5, 1)$	$b_3(0.5, 1.85)$
$c_1(0, 0.15)$	$c_2(0, 1)$	$c_3(0, 1.85)$



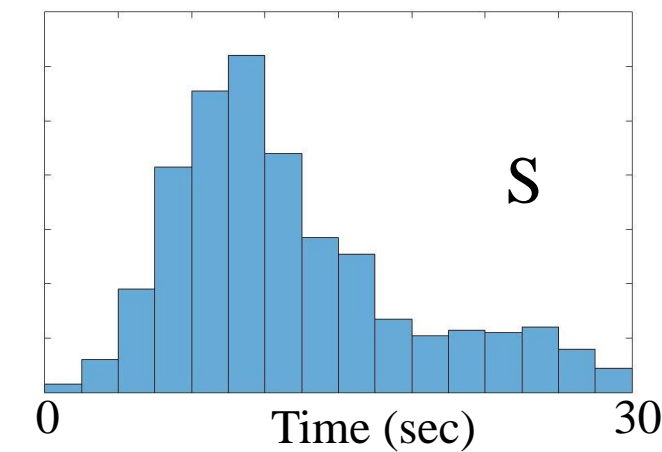
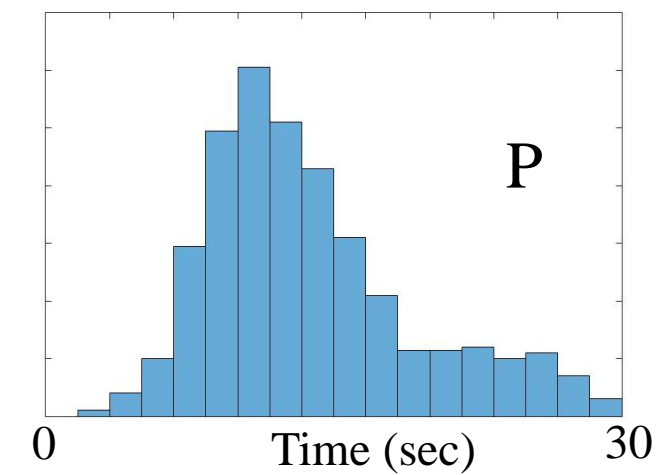
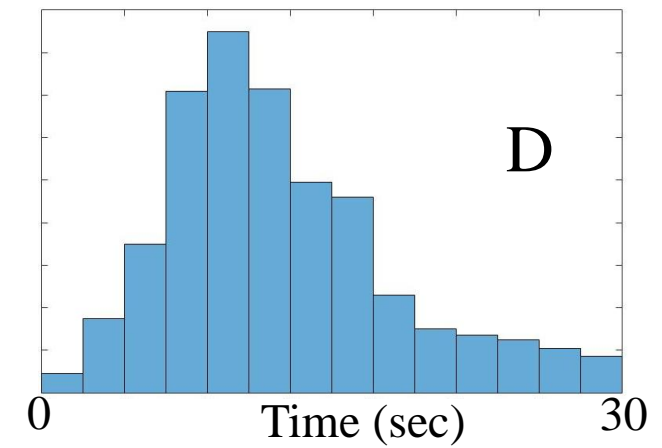
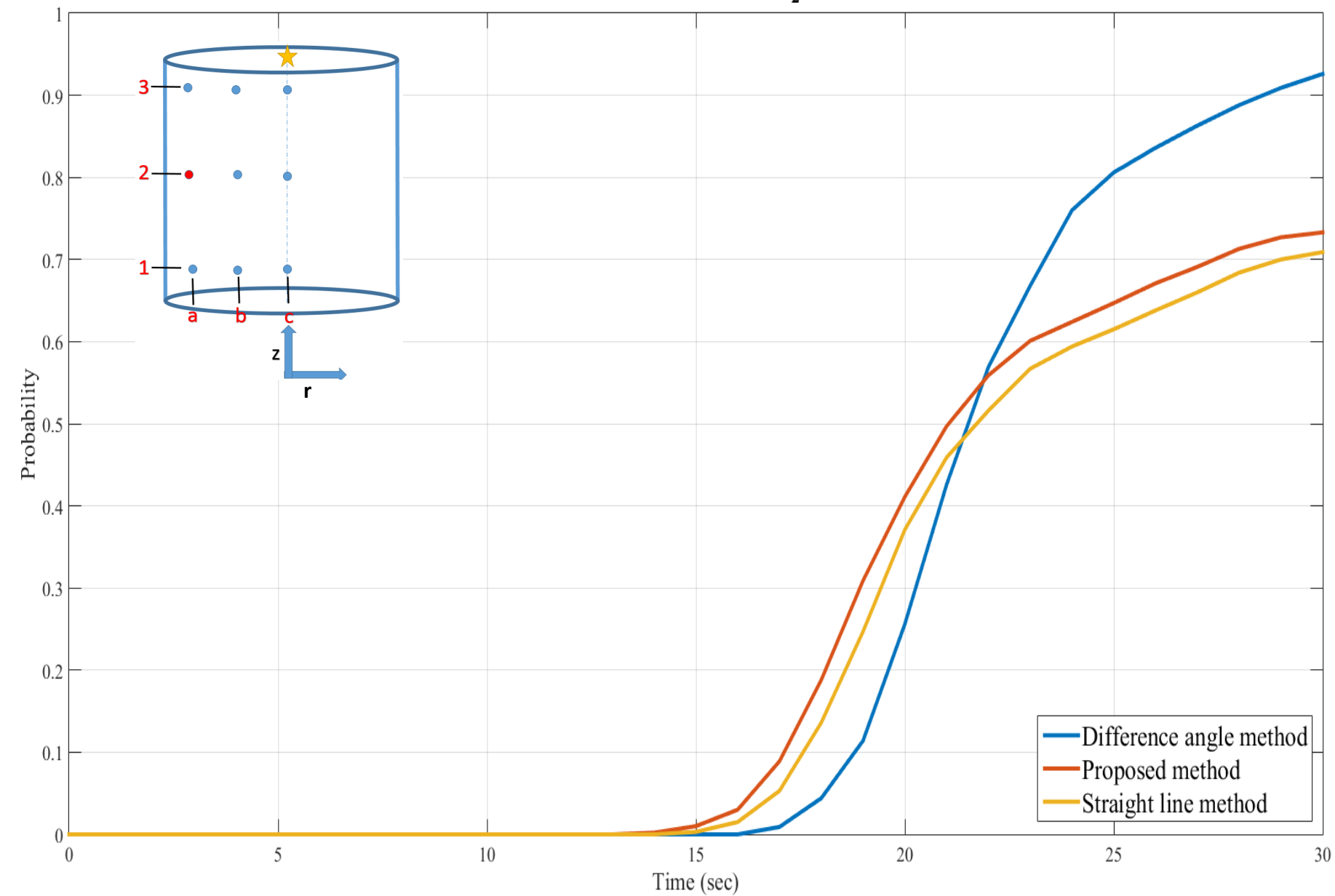
# Experiment I – Results from location $a_1$

## CDF from location $a_1$



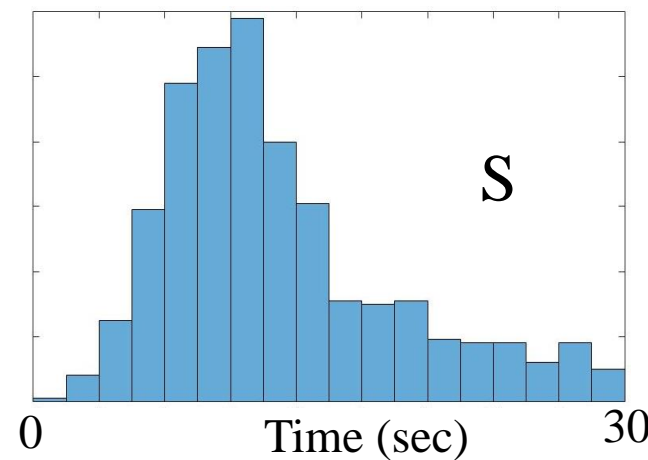
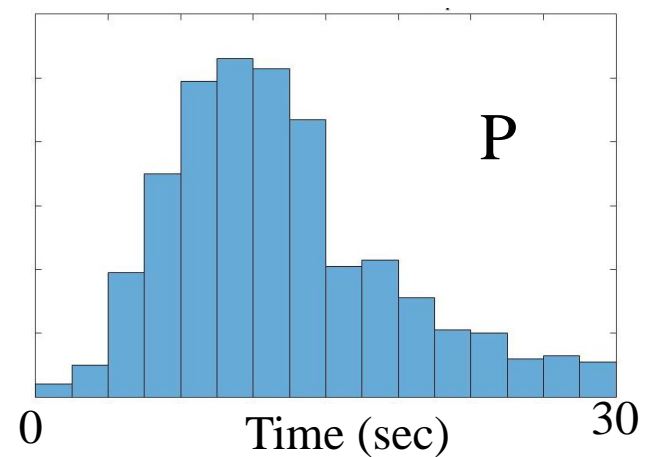
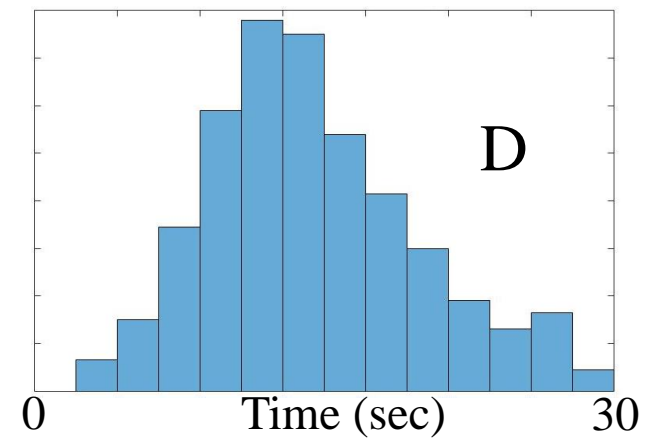
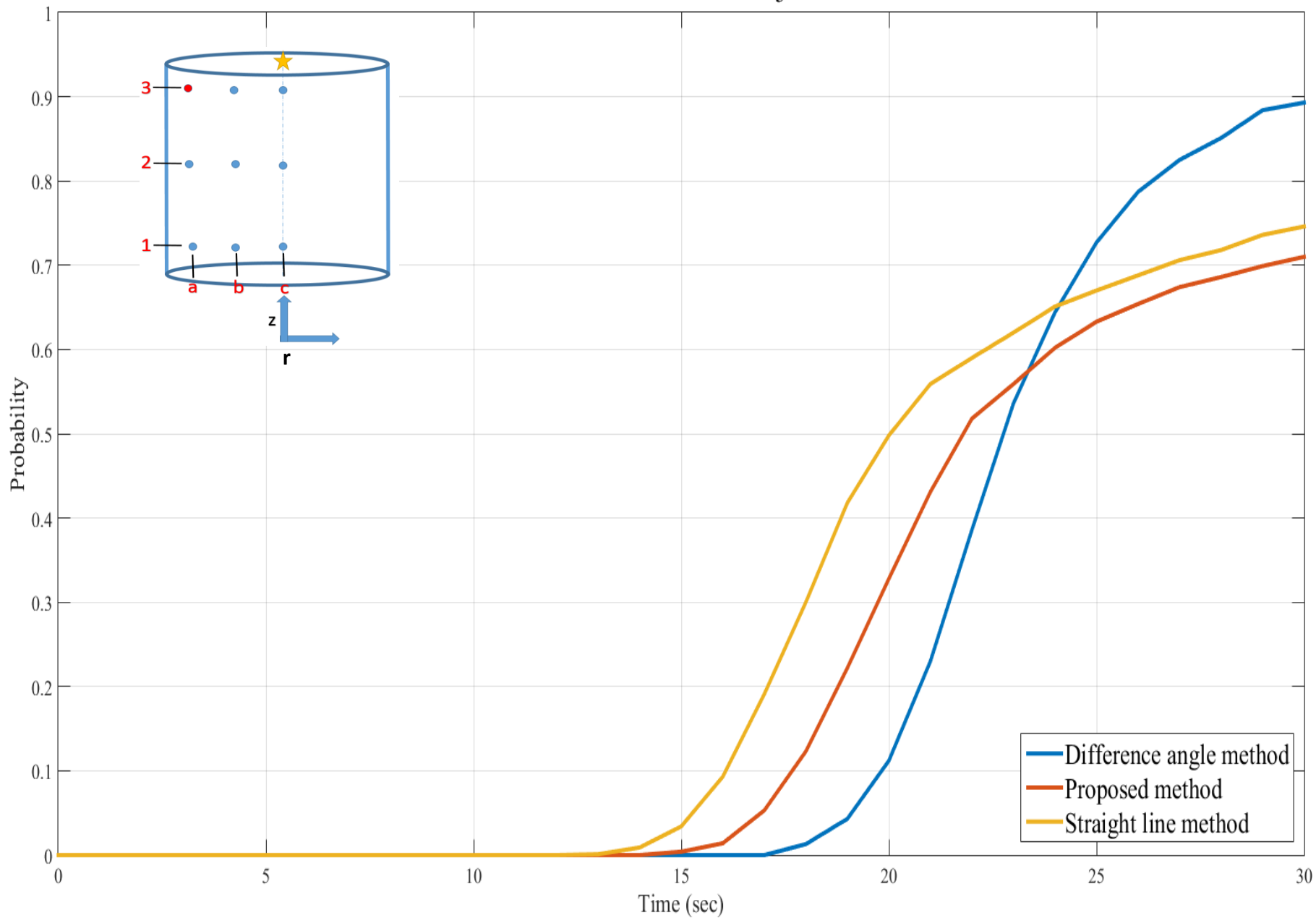
# Experiment I – Results from location $a_2$

CDF from location  $a_2$



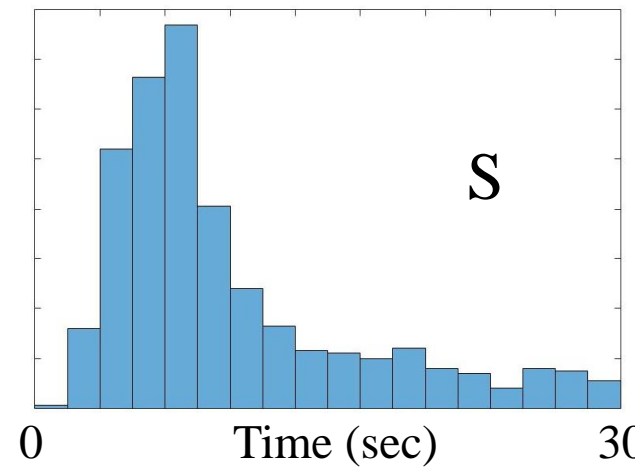
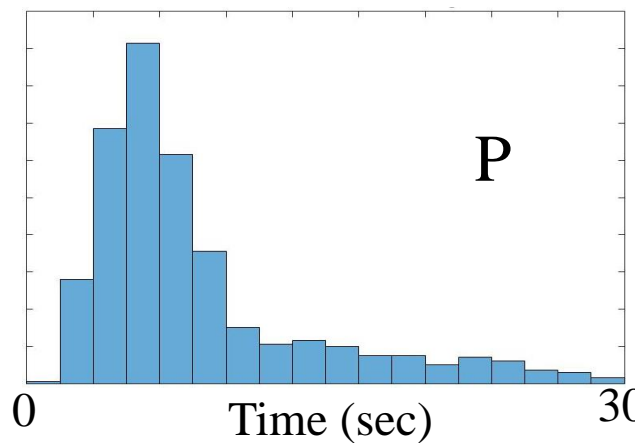
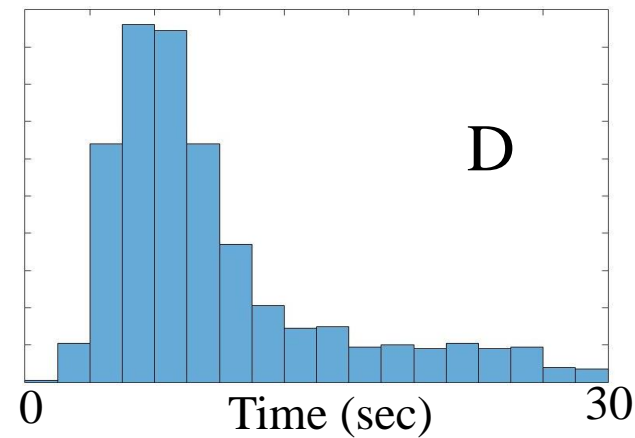
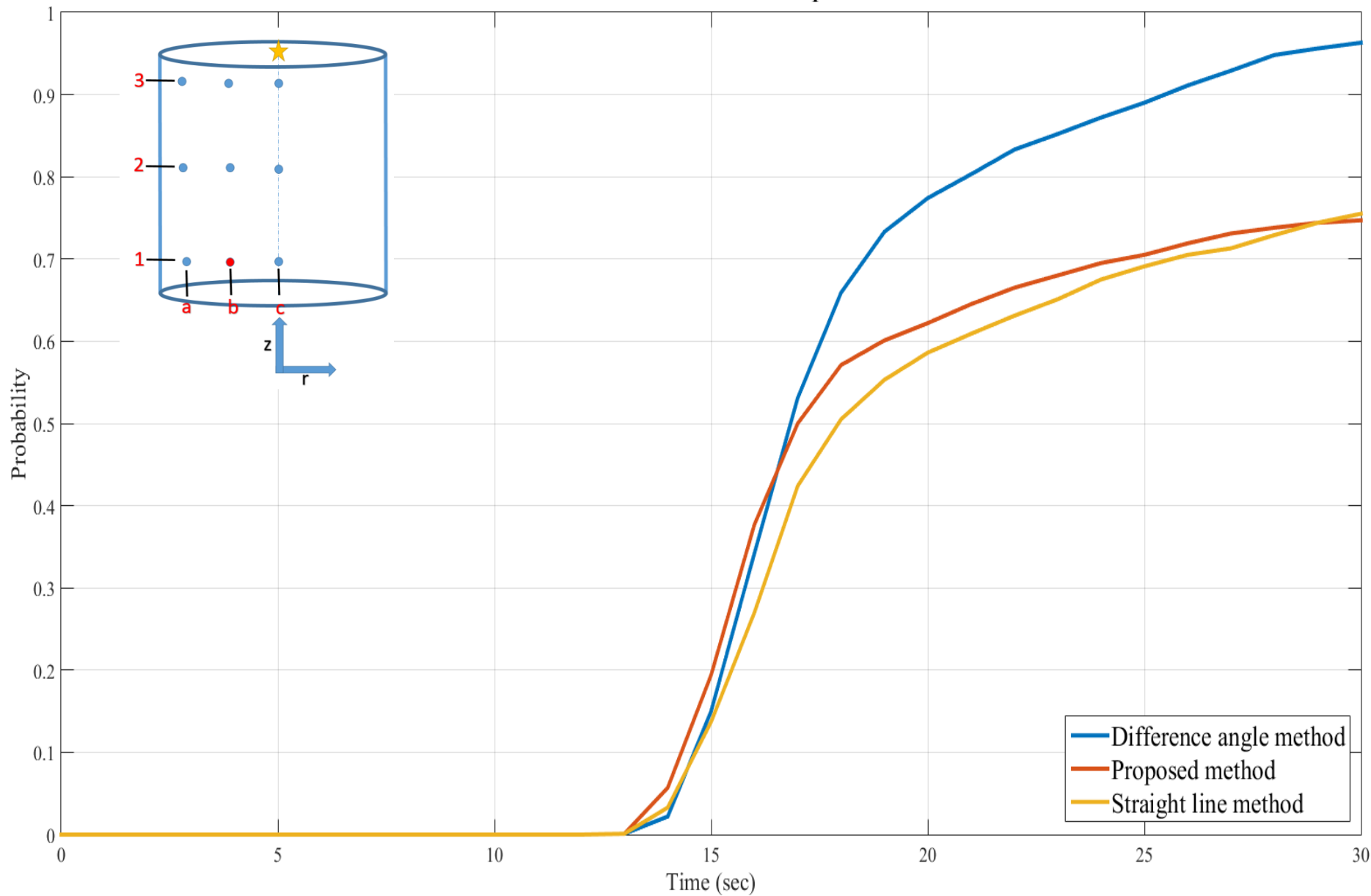
# Experiment I – Results from location $a_3$

CDF from location  $a_3$



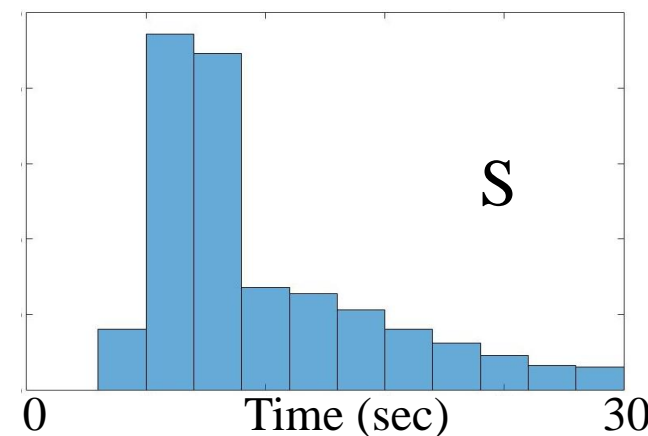
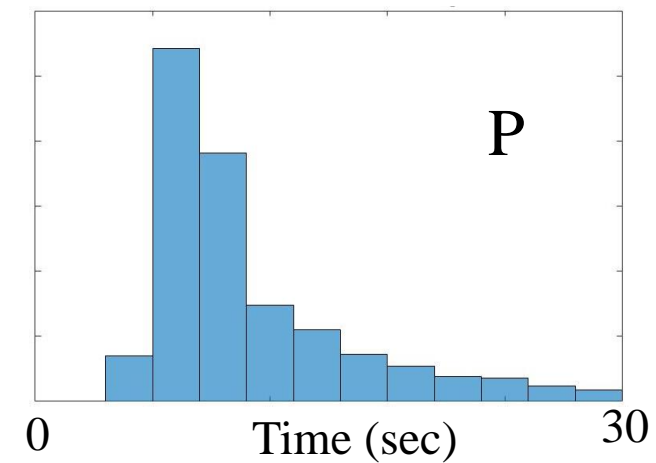
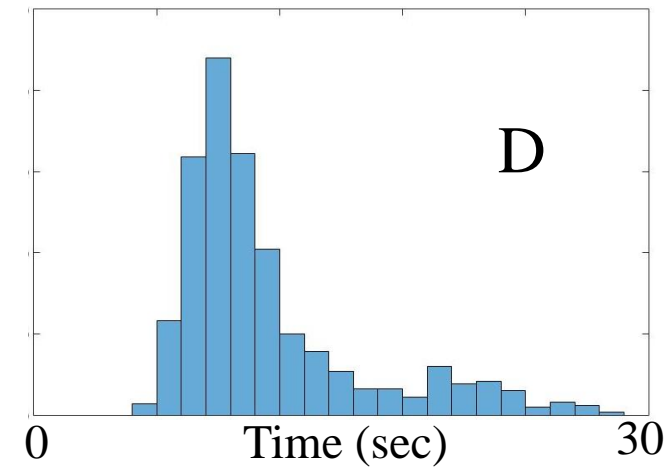
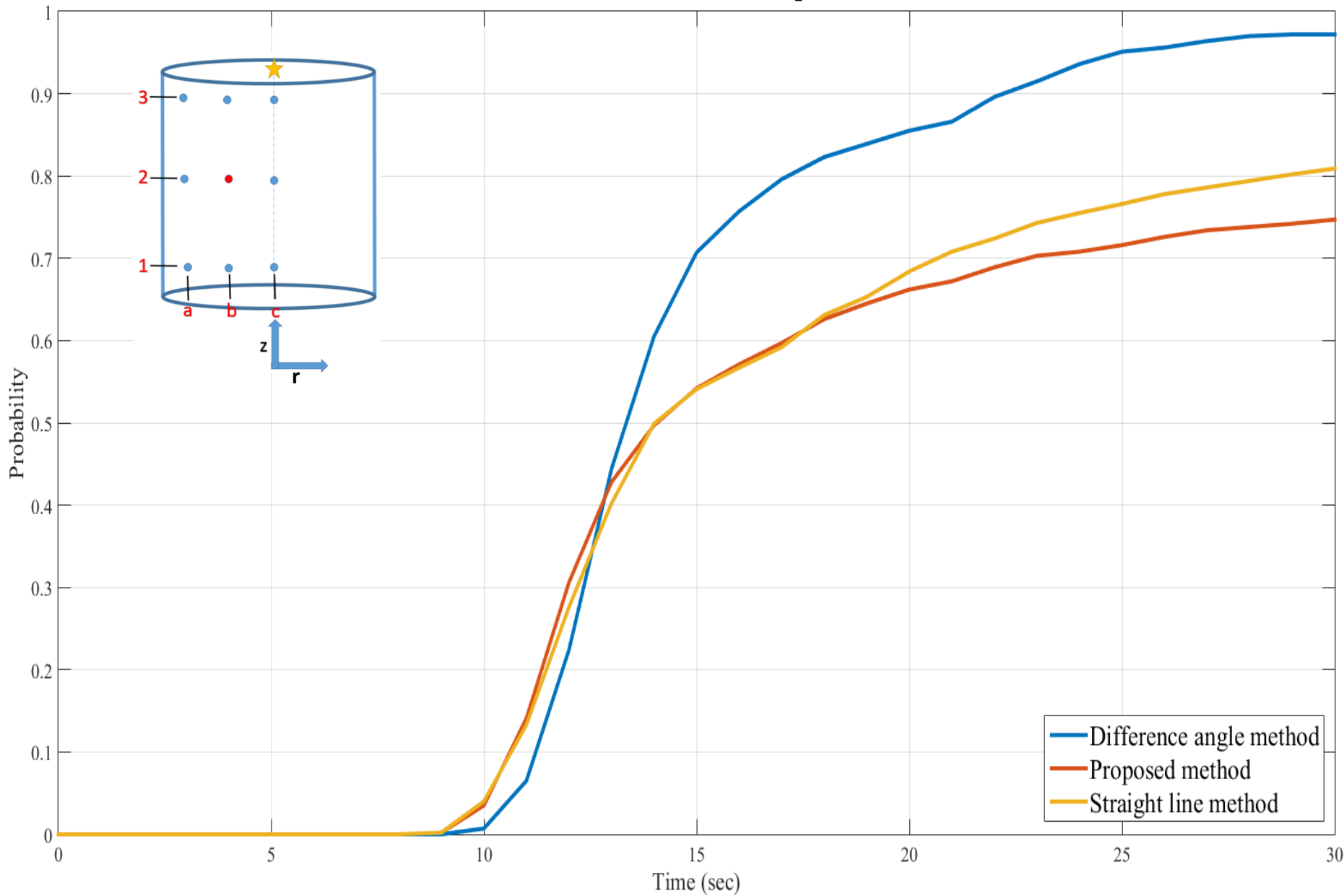
# Experiment I – Results from location $b_1$

## CDF from location $b_1$



# Experiment I – Results from location $b_2$

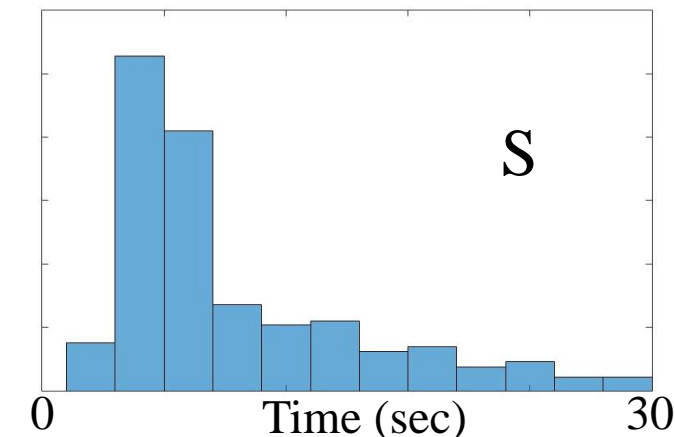
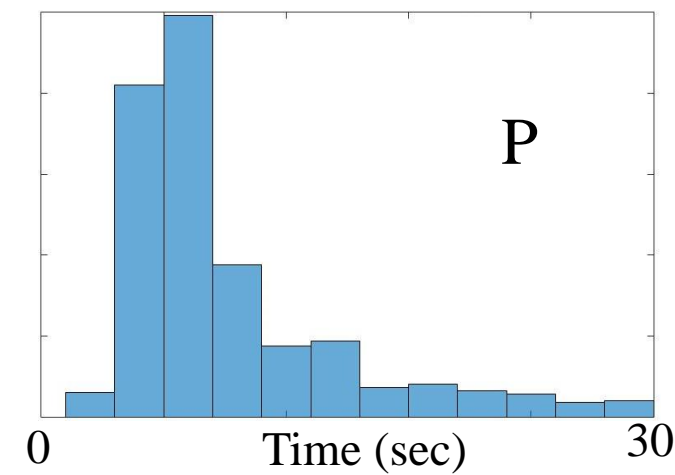
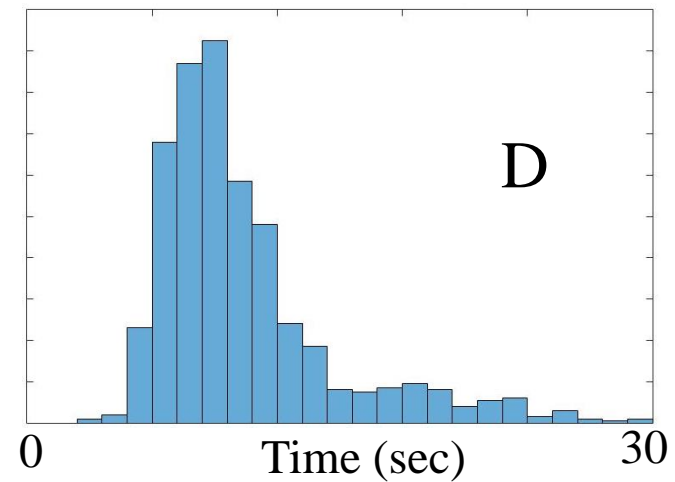
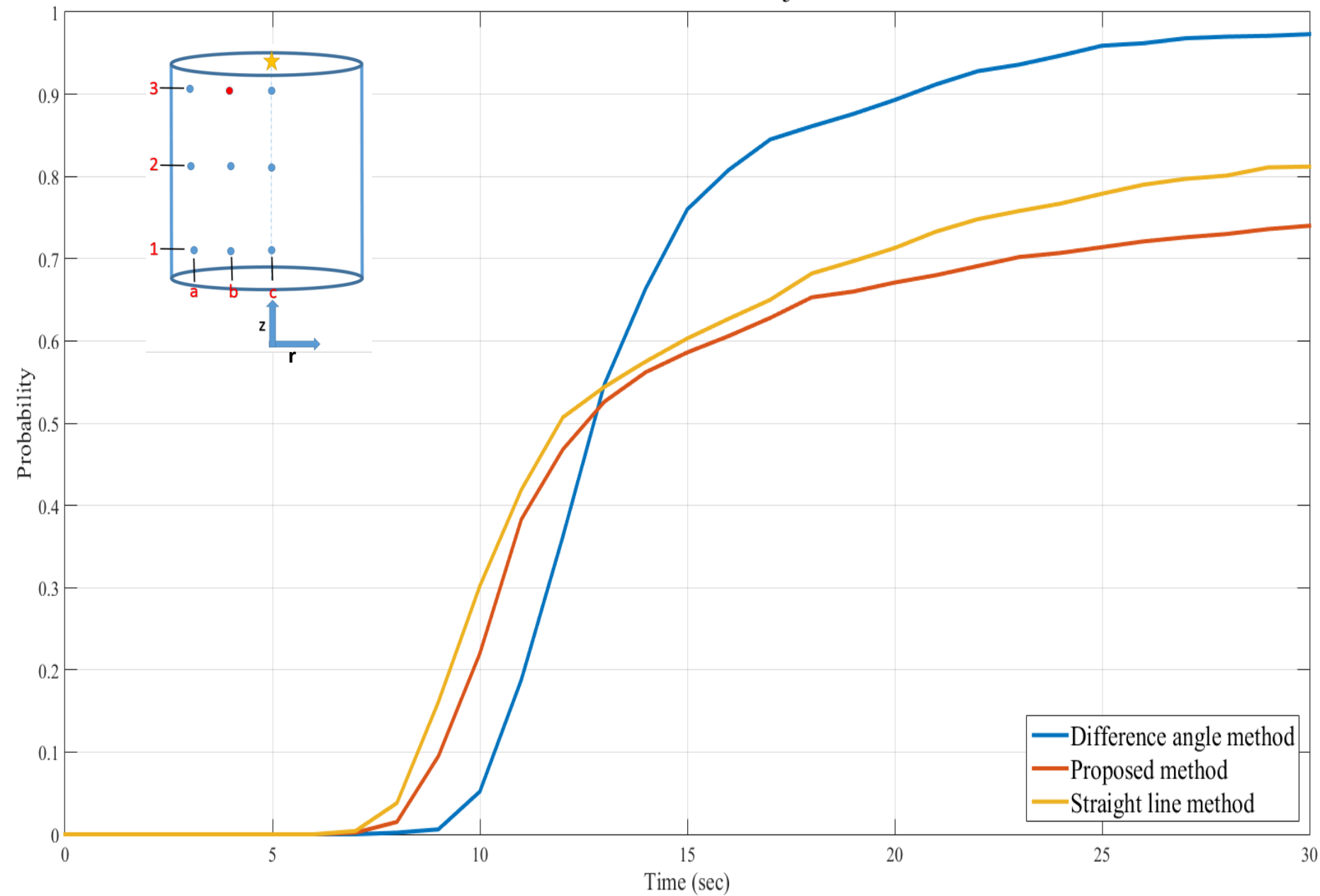
## CDF from location $b_2$





# Experiment I – Results from location $b_3$

CDF from location  $b_3$

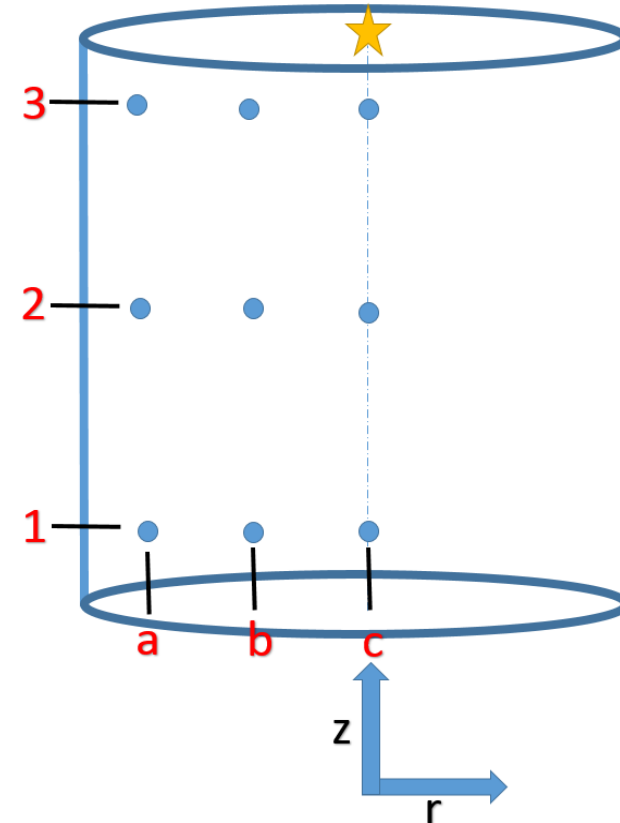


# Monte Carlo Experiments

Experiment II Setup:

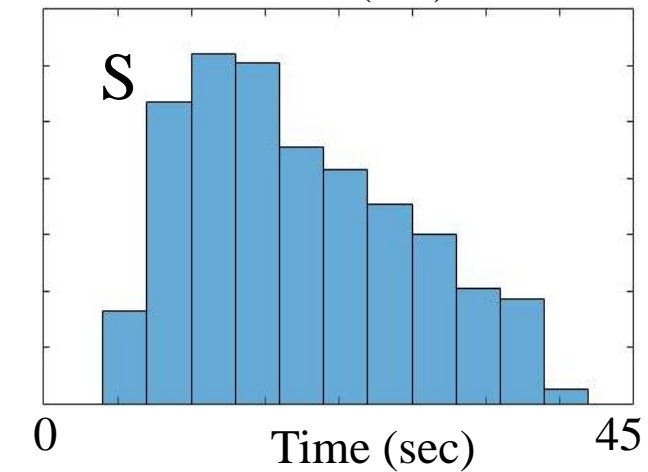
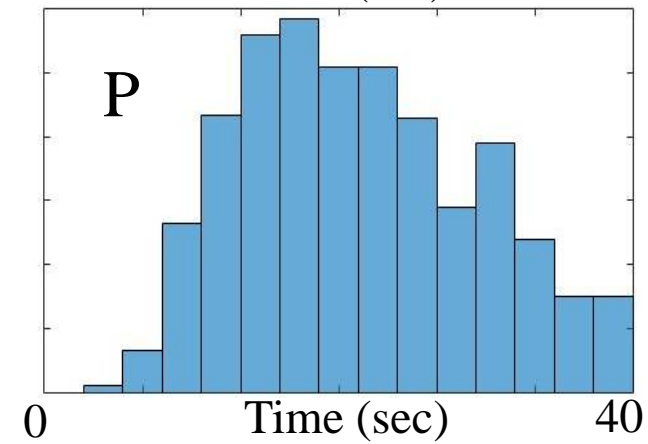
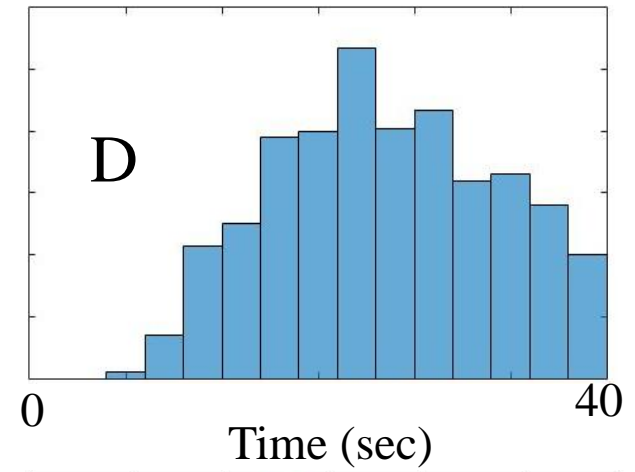
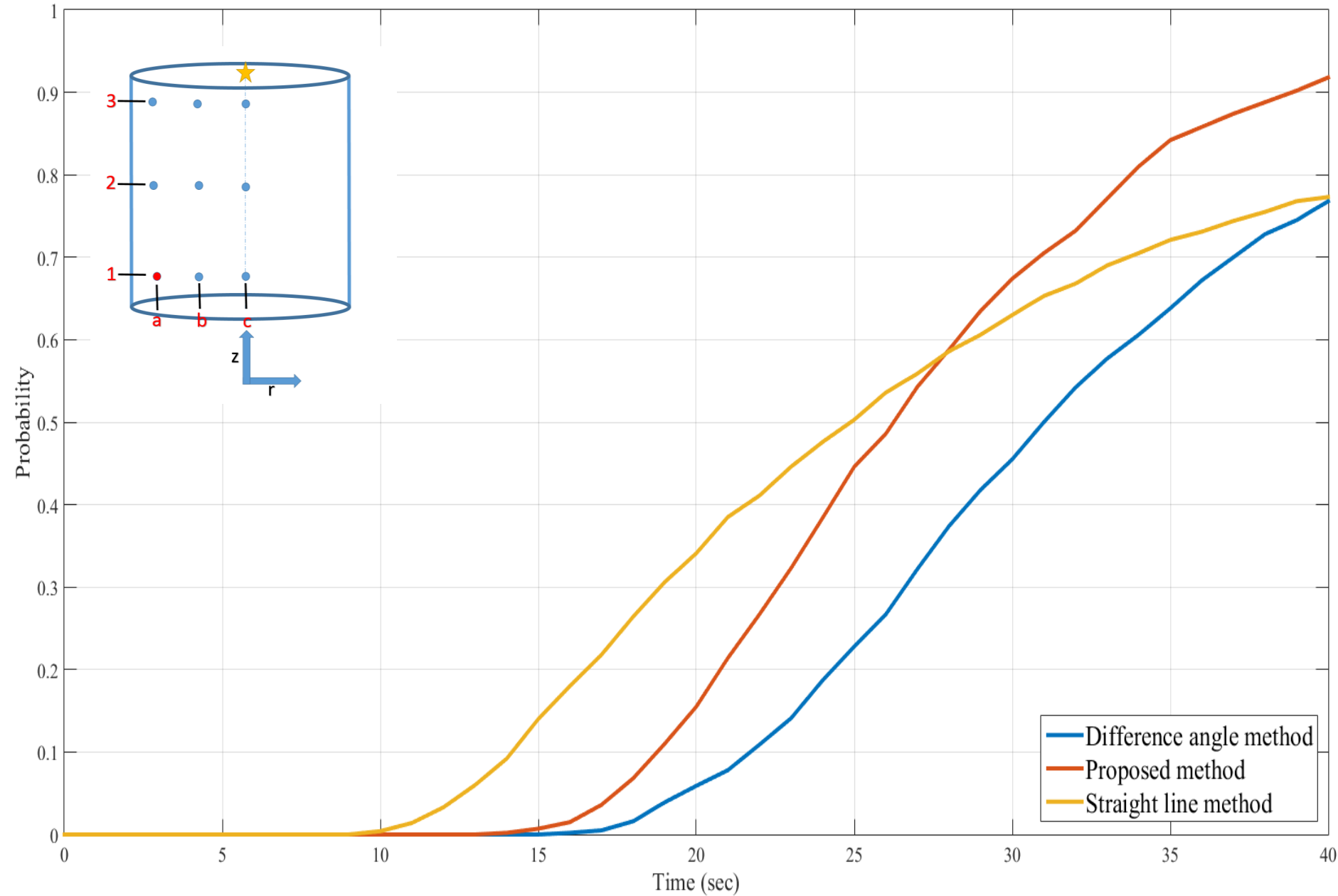
Experiment II
PD Controller (Constant Gains)
Disturbance: Mean=0, Variance=0.01
Scheduled Planner Gain
Docking region limit 0.043
Proposed method weights (A = 2, B =50)
Straight line method (A = 0, B =50)
Number of Monte Carlo runs : 1000

$a_1(0.95, 0.15)$	$a_2(0.95, 1)$	$a_3(0.95, 1.85)$
$b_1(0.5, 0.15)$	$b_2(0.5, 1)$	$b_3(0.5, 1.85)$
$c_1(0, 0.15)$	$c_2(0, 1)$	$c_3(0, 1.85)$



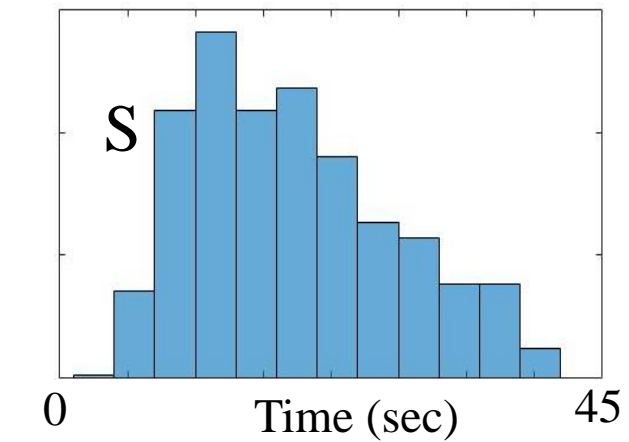
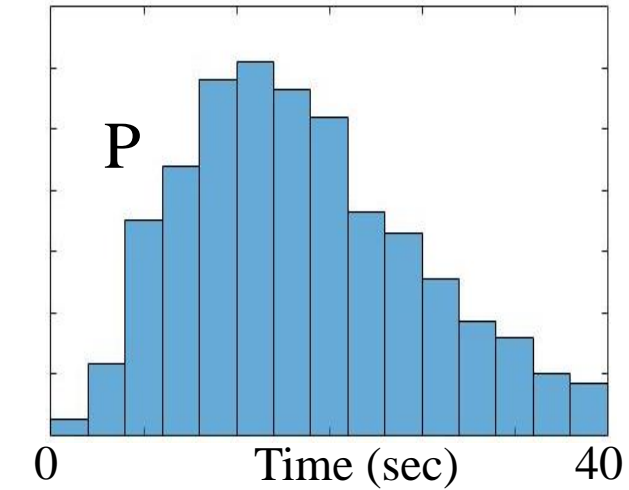
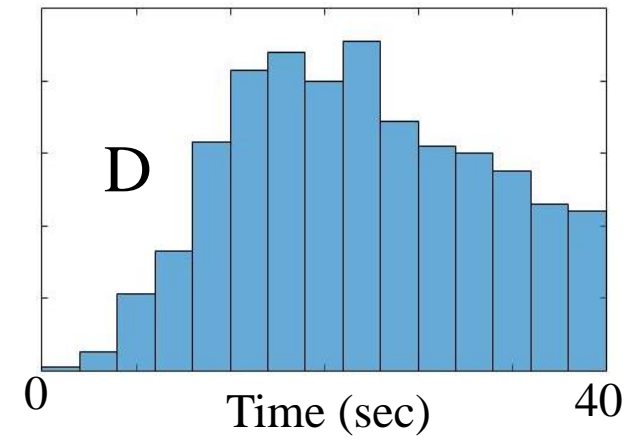
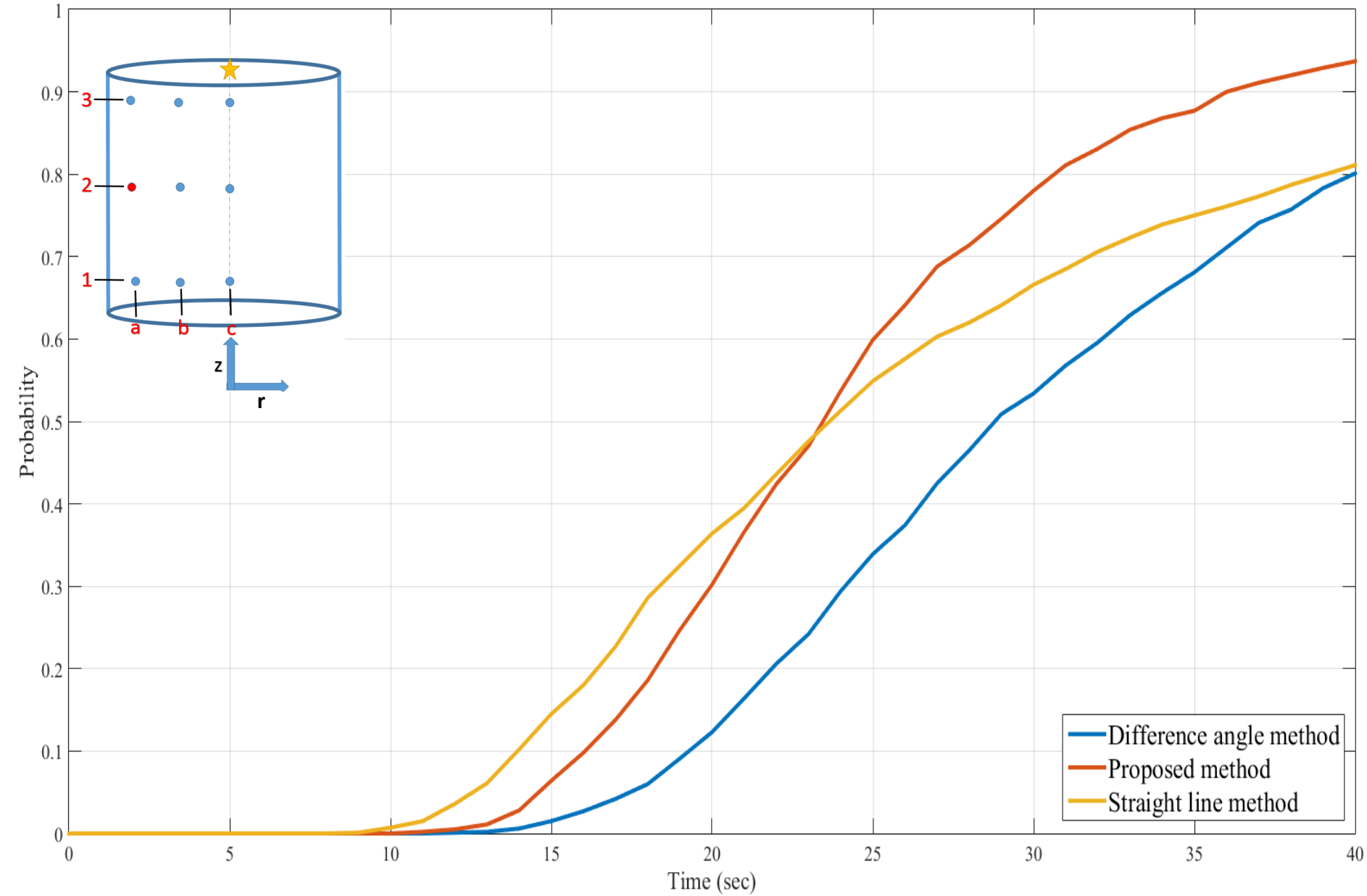
# Experiment II – Results from location $a_1$

## CDF from location $a_1$



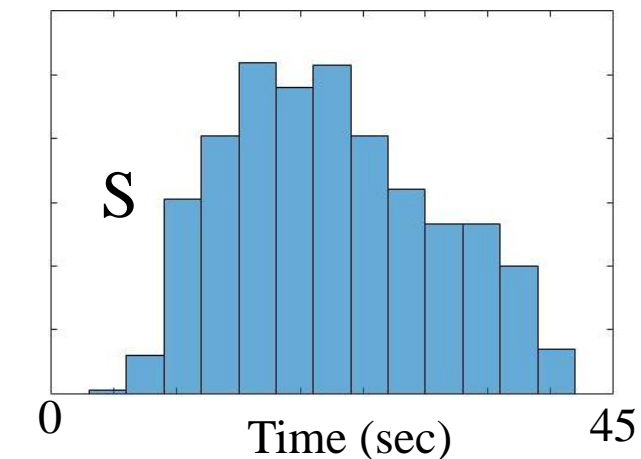
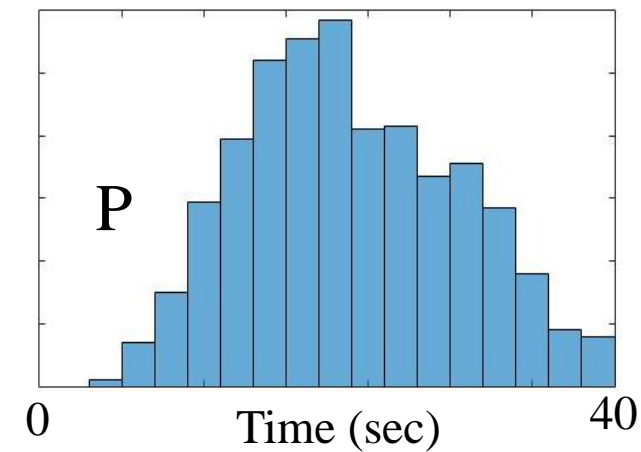
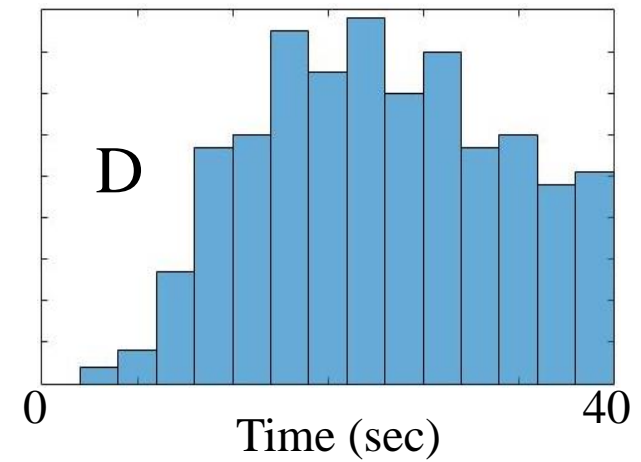
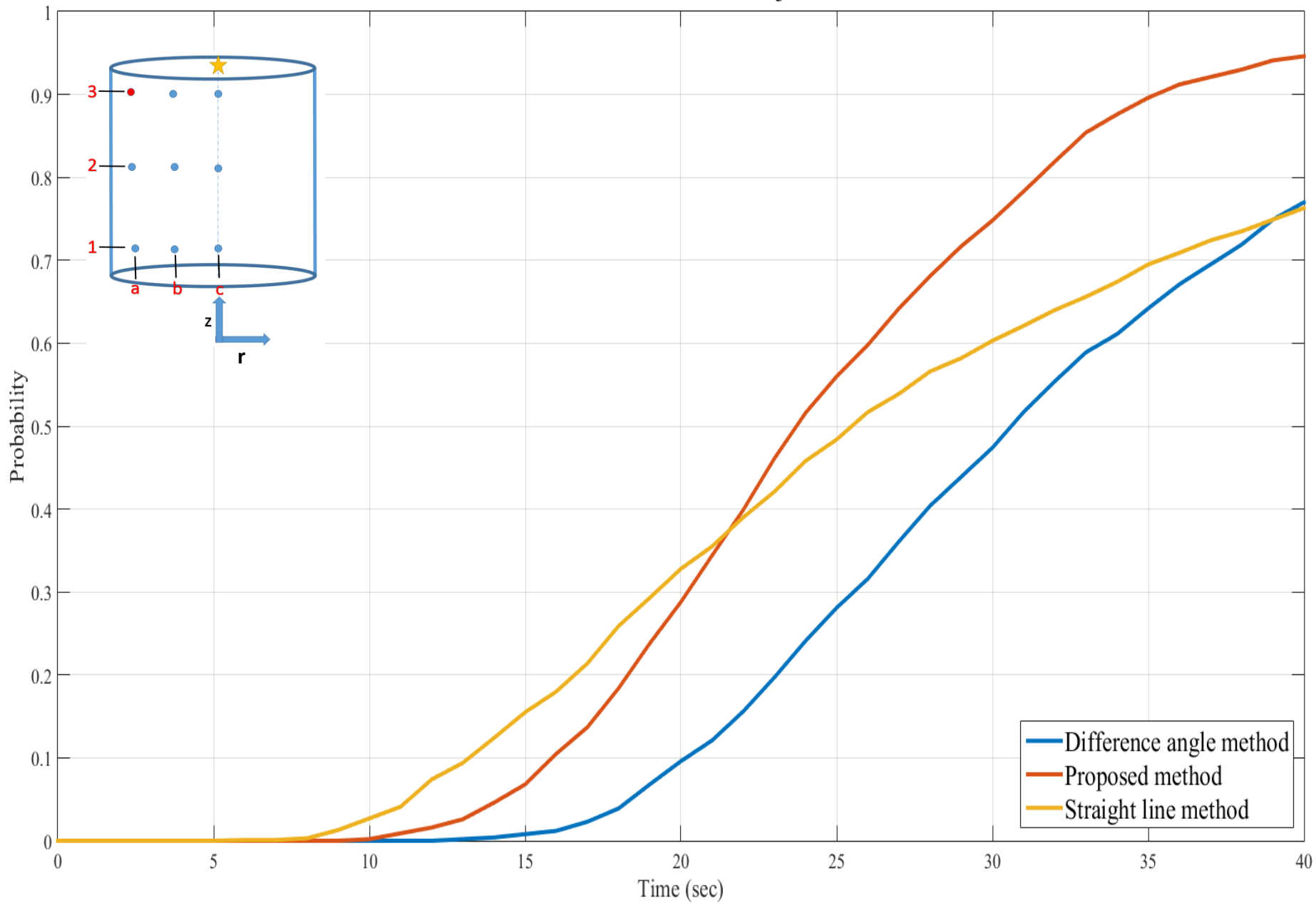
# Experiment II – Results from location $a_2$

## CDF from location $a_2$



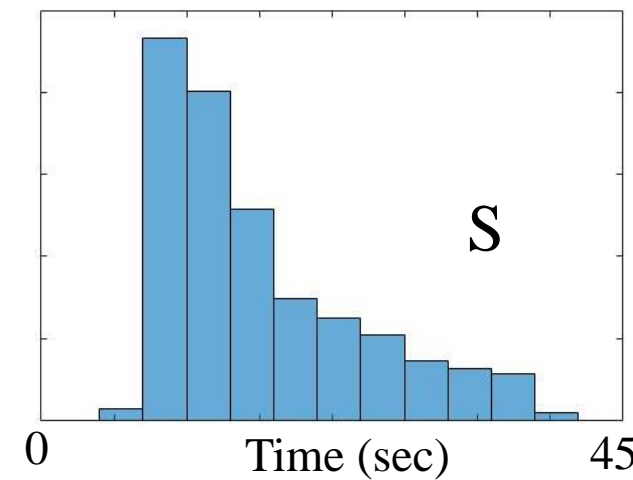
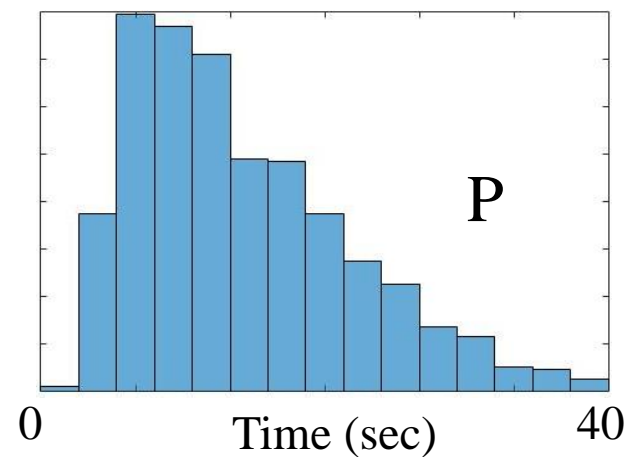
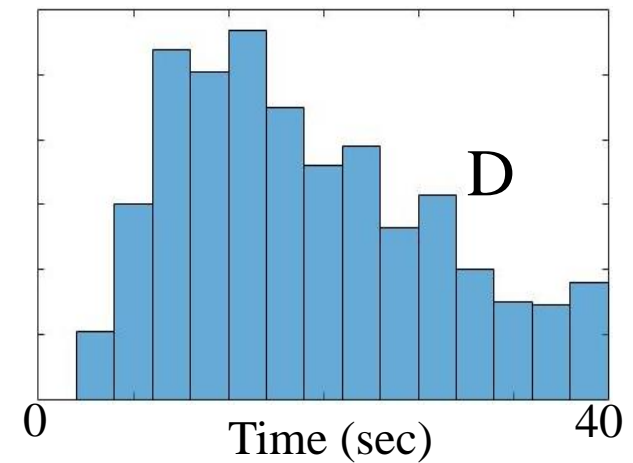
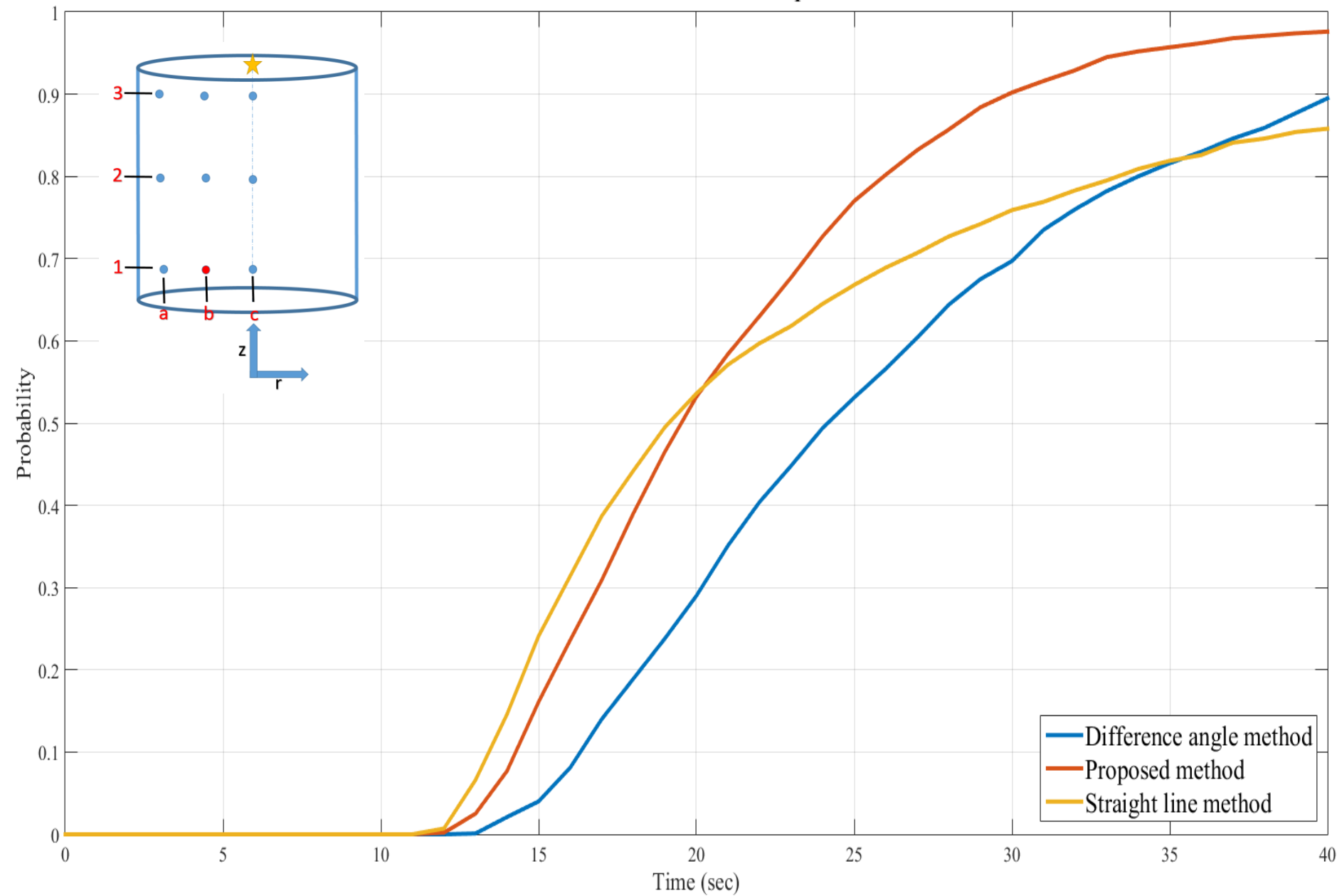
# Experiment II – Results from location $a_3$

## CDF from location $a_3$



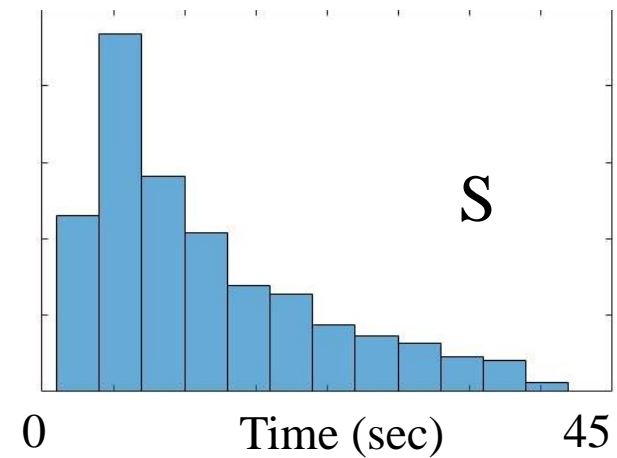
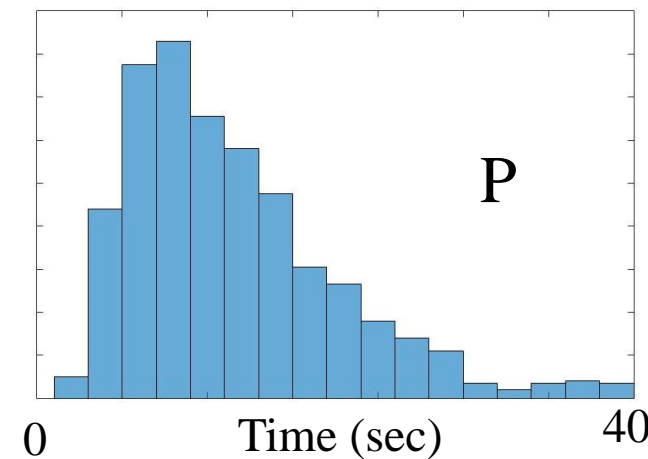
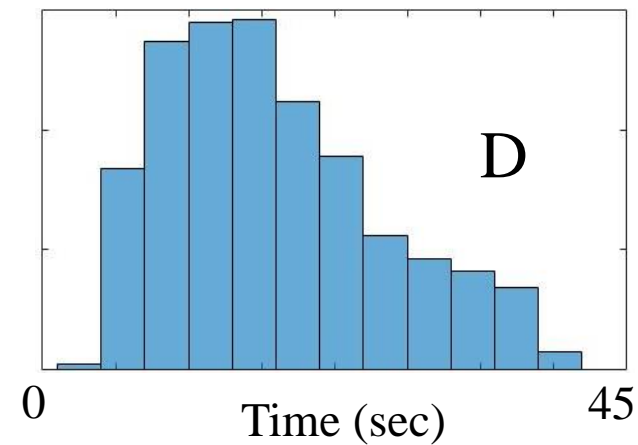
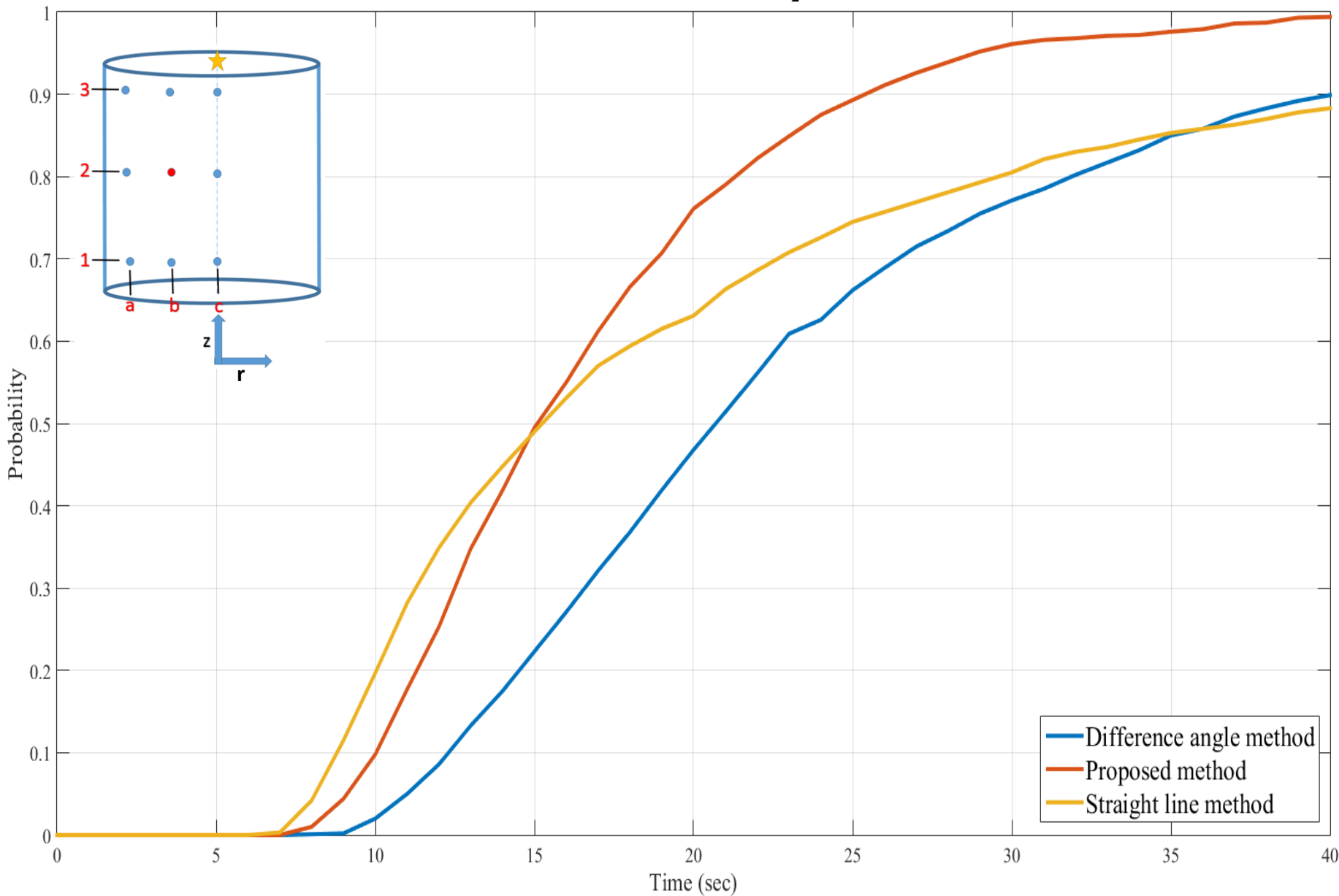
# Experiment II – Results from location $b_1$

## CDF from location $b_1$



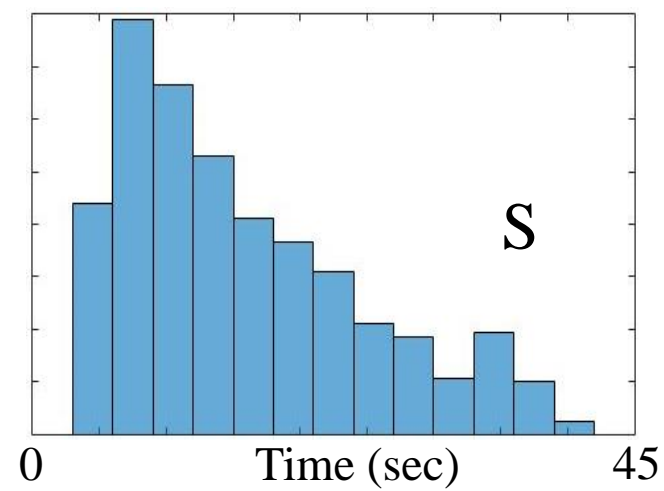
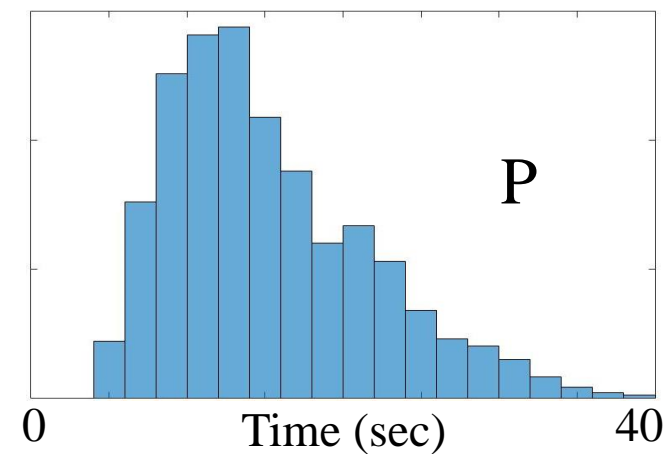
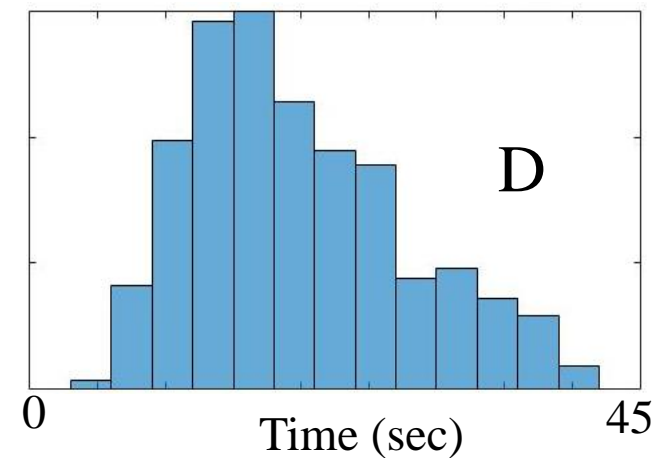
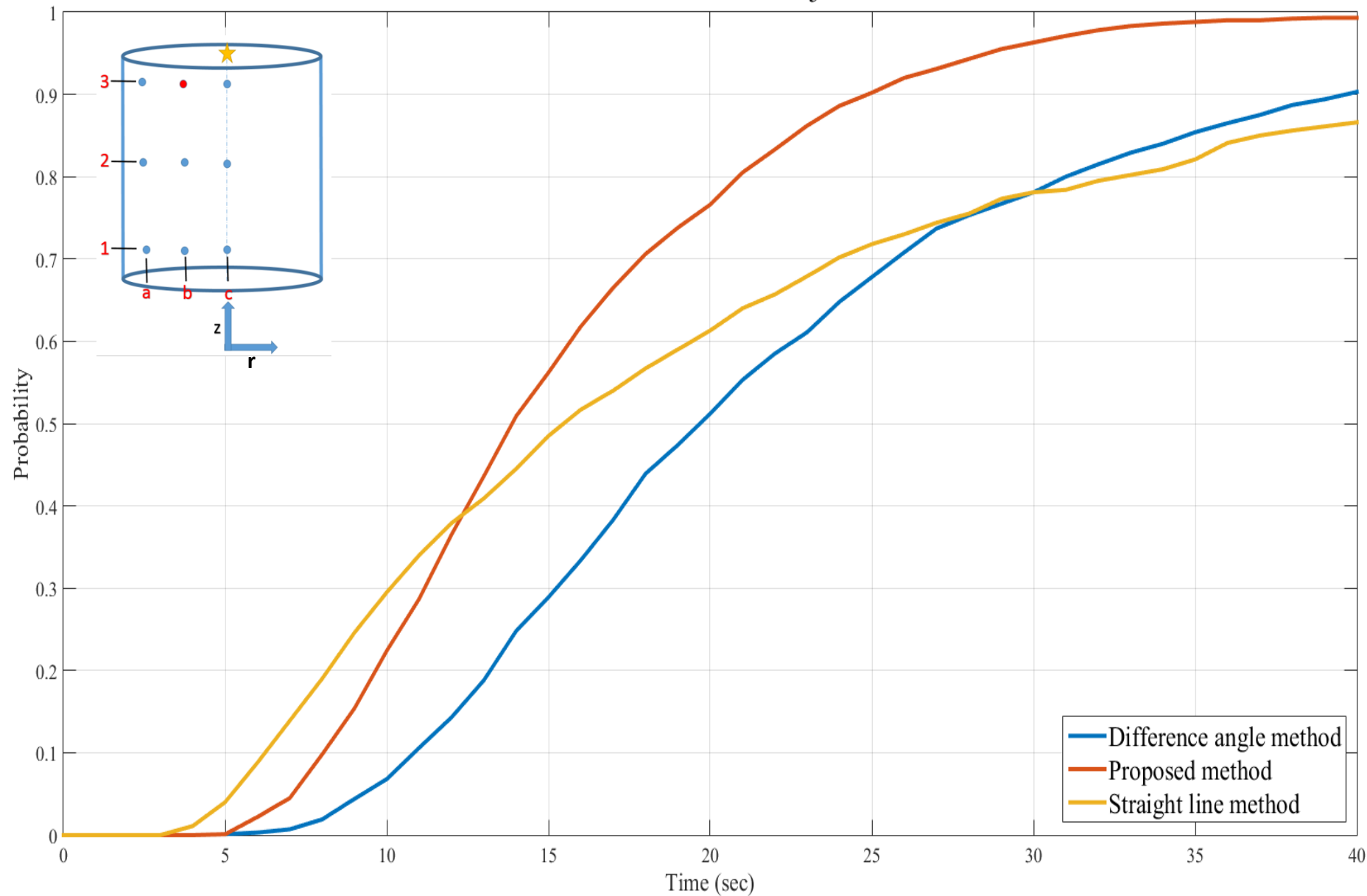
# Experiment II – Results from location $b_2$

## CDF from location $b_2$



# Experiment II – Results from location $b_3$

## CDF from location $b_3$





# Future Work

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- Simulations with other types of controllers
- Flight tests

